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11 **Chapter 19**
12 **Solar diurnal tides in the middle atmosphere:**
13 **Interactions with the zonal-mean flow, planetary**
14 **waves and gravity waves**

15 Ulrich Achatz, Fabian Senf and Norbert Grieger

16 **Abstract** The dynamics of solar tides is investigated with regard to variations of
17 the background atmosphere, including planetary waves (PW), and to the interac-
18 tion with gravity waves (GW). (1) Using a linear model with a clear cause-effect
19 relationship, it is shown that planetary waves play an important role in tidal dynam-
20 ics, most importantly by inducing non-migrating tidal components from a migrating
21 thermal forcing. (2) Ray-tracing simulations are used to analyze the GW force on
22 the large-scale flow including the solar tides. In comparison to classic GW param-
23 eterizations, the inclusion of time-dependence and horizontal refraction leads to a
24 significant decrease of the GW drag.

25 **19.1 Introduction**

26 The diurnal cycle of solar heating represents a forcing of the atmosphere at the di-
27 urnal period (24h) and its higher harmonics. Corresponding large-scale waves, i.e.
28 solar tides, are emitted, with signatures in all dynamic fields, including wind and
29 temperature, propagating upwards into the mesosphere/lower thermosphere (MLT)
30 region (*Chapman and Lindzen, 1970*). Due to the enormous density decrease tidal
31 amplitudes grow significantly so that they represent a major component of atmo-
32 spheric variability in the MLT. Tides are very sensitive to the propagation conditions

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33 they encounter on their way from the forcing region. Hence, if the mean atmospheric
 34 circulation is modified by solar variability this could leave a significant footprint on
 35 the tides encountered in the MLT. Moreover, many processes, discussed in this book,
 36 by which solar variability could have an impact on the tropopause region and below,
 37 rely on dynamic coupling mechanisms between the lower atmosphere and higher
 38 regions where the influence of a varying sun acts primarily. It seems important to
 39 understand these well. Solar tides, however, are controlled just by such mechanisms
 40 so that research on tides might be helpful not only for the detection whether solar
 41 variability can influence the lower layers of the atmosphere, but also for a better
 42 understanding how this might happen. We here take the chance to summarize re-
 43 cent work within this framework (Achatz et al., 2008; Achatz et al., 2010; Senf and
 44 Achatz, 2011). Therein the focus mainly is on how much various processes and
 45 mechanisms contribute to the tidal signature in the MLT.

46 One of these is the diurnal cycle of atmospheric heating. Two of the main heating
 47 processes subject to a significant diurnal cycle, and contributing to solar tides in the
 48 MLT, are the direct absorption of solar radiation by ozone in the stratosphere and
 49 by water vapor in the troposphere. This is supplemented by the diurnal cycle of
 50 tropospheric latent heat release and convection, mostly over tropical land masses.
 51 In propagating from the regions of these source processes to the MLT solar tides
 52 encounter propagation conditions which can have a strong impact on them. Here
 53 one discriminates between the impact of the zonal mean of the atmosphere on tides,
 54 which cannot change their zonal wave number, and the interaction between tides
 55 and planetary waves, which can do so. In general, the spatial and time dependence
 56 of the signature of the solar tides in any dynamic variable X is given by

$$\begin{aligned}
 X(\lambda, \phi, z, t) = & \sum_{n=1}^{\infty} \left\{ A_{n,0}(\phi, z) \cos(n\Omega t - \Phi_{n,0}^e) \right. \\
 & \left. + \sum_{s=1}^{\infty} [A_{n,s}^e(\phi, z) \cos(n\Omega t - s\lambda - \Phi_{n,s}^e) + A_{n,s}^w(\phi, z) \cos(n\Omega t + s\lambda - \Phi_{n,s}^w)] \right\} \quad (19.1)
 \end{aligned}$$

57 Here λ and ϕ denote the geographic longitude and latitude, respectively. The al-
 58 titude is given by z , and t is the universal time. The rotation rate of the earth is
 59 $\Omega = 2\pi/24\text{h}$. The temporal subharmonics corresponding to $n = 1, 2, 3$ are the diur-
 60 nal, semidiurnal, and terdiurnal tide, respectively. Each is decomposed into a zon-
 61 ally symmetric part, with zonal wave number $s = 0$, and east- and westward trav-
 62 eling components at zonal wave numbers $s > 0$ with amplitudes $A_{n,s}^e$ and $A_{n,s}^w$, and
 63 phases $\Phi_{n,s}^e$ and $\Phi_{n,s}^w$, respectively, both depending both on latitude and altitude. For
 64 conciseness, a westward or eastward traveling diurnal component at wave number
 65 s will be called DWs or DEs, respectively. The name for the corresponding zon-
 66 ally symmetric component is DS0. Since the apparent movement of the sun around
 67 the globe is westward, a leading tidal component of each temporal subharmonic is
 68 the westward traveling one at zonal wave number $s = n$, called the migrating tide.
 69 Its horizontal propagation is synchronous with that of the sun. Since also the tidal
 70 forcing by the diurnal cycle of solar heating can be decomposed into migrating and

71 non-migrating components, the question arises which tidal components eventually
 72 dominate when the thus forced waves propagate into the MLT. Consider the interac-
 73 tion between tides and large-scale stationary planetary waves in terms of wave-wave
 74 interactions, governed by the triad condition $s_2 = s_1 \pm m$, with $s_{1,2}$ being zonal wave
 75 numbers of the tide and its forcing, and m the zonal wave number of a planetary
 76 wave. Clearly, a planetary wave can lead to the emergence of a non-migrating tide
 77 in the MLT from a migrating forcing further below, while the zonal-mean part of
 78 the atmosphere, with zonal wave number $m = 0$ cannot do so. Note that these are
 79 mechanisms already captured by a linear model where the dynamics of solar tides
 80 is represented after a linearization about an atmospheric reference state containing
 81 both zonal mean and stationary planetary waves.

82 While already the above leads to interesting questions, i.e. how much does each
 83 tidal forcing contribute to the total tidal signal, and how do interactions between
 84 tides and zonal mean or planetary waves influence what finally emerges as tide in
 85 the MLT, this is by far not all. Upward propagating small-scale gravity waves (GWs)
 86 transport a significant amount of momentum and energy from the lower to the mid-
 87 dle atmosphere (*Fritts and Alexander, 2003*). Again due to the density decrease the
 88 GW amplitude rises in the course of their propagation from the troposphere to the
 89 MLT so that they eventually become unstable and break. Because solar tides, mainly
 90 their horizontal winds, induce changes in the GW propagation and properties, e.g.
 91 in GW vertical wave number, the wave breaking itself and the resulting momentum
 92 deposition (*Lindzen, 1981*) are periodically modulated. This way results a diurnal
 93 variation of the GW force on the large-scale flow which can have a feedback on the
 94 tides. This effect of gravity waves on thermal tides has not been well understood
 95 so far (*Ortland and Alexander, 2006*). Many linear models for the description of
 96 solar tides incorporate it by simple Rayleigh friction, which most likely is a crude
 97 over-simplification, needing either verification or replacement by better approaches.

98 These issues are addressed in the work reported here. We sketch in section 19.2
 99 some steps and results in the research on the impact of zonal-mean and planetary-
 100 wave background variations on solar tides, give an account of new findings on in-
 101 teraction between tides and GWs in section 19.3, and finally summarize in section
 102 19.4. All of the work reported here exclusively addresses the diurnal tide.

103 **19.2 The seasonal cycle of the diurnal solar tide in its interaction** 104 **with zonal-mean variations and planetary waves**

105 The effect of the interaction between tidal forcing, migrating and non-migrating,
 106 and zonal-mean atmosphere or planetary waves on the various diurnal tidal com-
 107 ponents has been an original focus of research (*Hagan and Roble, 2001; Grieger*
 108 *et al., 2004, e.g.*). Its modulation by the seasonal cycle represents an important test
 109 of our current understanding of tidal dynamics, and therefore has more recently
 110 attracted considerable attention. The MLT amplitude of the migrating diurnal tide
 111 exhibits a strong semiannual variation with maxima at equinox and minima at sol-

112 stice. *McLandress* (2002a,b) explains this in terms of the impact of the seasonally
113 varying zonal-mean wind on the tidal propagation conditions. The seasonal cycle
114 of the leading non-migrating tides (DE3, DS0, and DW2) in the MLT has been
115 addressed by *Oberheide et al.* (2005, 2006). They follow a similar strategy to the
116 one from *Hagan and Roble* (2001) in using a linear model (GSWM) and a gen-
117 eral circulation model (TIME-GCM) for simulating the seasonal cycle. The latter
118 has a lower boundary at 30km altitude, where a migrating diurnal tide was pre-
119 scribed, as obtained from the linear model, which again has a zonally symmetric
120 background. The TIME-GCM is then integrated with prescribed planetary wave
121 activity at the lower boundary. To some degree the two models complement each
122 other: The linear GSWM captures the direct effect from the non-migrating forcing
123 in a zonally-symmetric background while the TIME-GCM, without non-migrating
124 forcing, can only produce non-migrating tides by an interaction between migrating
125 tides and planetary waves. The linear model is reported to reproduce the seasonal
126 cycle of DE3. This component therefore seems to result directly from a tide be-
127 ing forced by non-migrating heating, due to latent heat release, and its propagation
128 through the zonal-mean background atmosphere. An open question is which part
129 both factors play in comparison in determining the seasonal cycle of DE3. In the
130 same studies both the linear GSWM and the nonlinear TIME-GCM yield season-
131 ally varying components DS0 and DW2. Therefore, the excitation of DS0 and DW2
132 seem to be controlled by two processes, the interaction of migrating forcing and
133 planetary waves, and the direct non-migrating forcing in interaction with a varying
134 zonal mean in the background atmosphere. However, the respective role of varia-
135 tions in the zonal-mean background and the non-migrating forcing is not clarified
136 within GSWM. Moreover, the TIME-GCM integrations are fully nonlinear; corre-
137 sponding feedbacks are not excluded. It is therefore not possible to simply add the
138 GSWM result to the one from the GCM so as to obtain the complete tidal signal. A
139 more conclusive picture could arise from a linear model with a background atmo-
140 sphere incorporating the most important stationary planetary waves. Such analysis
141 have been done by *Achatz et al.* (2008).

142 Their model uses the primitive equations, linearized about a time-independent,
143 but fully three-dimensional, background atmosphere, with a spectral discretization
144 in the horizontal (T14) and 60 hybrid-coordinate layers in the vertical between
145 the ground and about 140km altitude. Sub-grid-scale processes are parameterized
146 crudely by vertically dependent Rayleigh friction, Newtonian cooling and horizon-
147 tal diffusion. The model is forced by diurnal oscillations in the heat sources, taken,
148 just as the background atmosphere, from the monthly climatology of a state-of-the-
149 art GCM HAMMONIA (*Schmidt et al.*, 2006) ranging from the ground far into
150 the thermosphere. The heat sources comprise, among others, the absorption of sol-
151 ar radiation, including the ultraviolet and extreme ultraviolet wavelength regime,
152 long-wave radiation, and heating by latent heat release and convection. Instead of a
153 brute forward integration, the equations including the forcing are Fourier analyzed
154 in time, so that for each tidal period a system of linear equations is obtained, which
155 are solved iteratively by a preconditioned conjugate gradient solver. The result is
156 the complete three-dimensional tidal structure, with all migrating and non-migrating

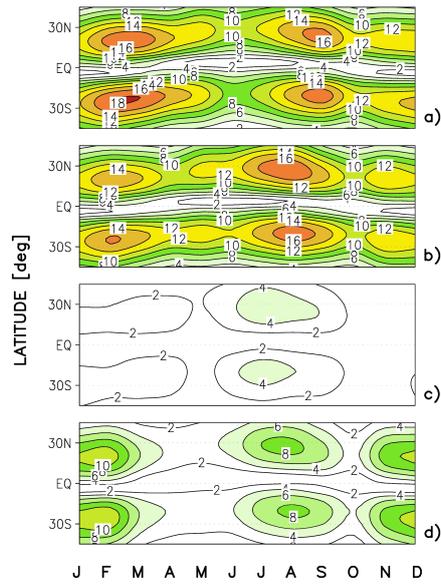


Fig. 19.1 From the linear model, the seasonal cycle in the amplitudes of the non-migrating component DW2 of the diurnal tide in the meridional wind at 95km altitude (a), the part due to variations of the background atmosphere (b), the part due to the seasonally varying part of the diurnal heat sources (c), and the corresponding contribution from the seasonal cycle of the stationary planetary waves (d). Units are m/s. Taken from Achatz, U., N. Grieger, and H. Schmidt, *Mechanisms controlling the diurnal solar tide: Analysis using a GCM and a linear model*, *J. Geophys. Res.*, 113, A08,303, 2008. Copyright 2008 American Geophysical Union. Modified by permission of American Geophysical Union.

157 components. Note that the background state is three-dimensional so that the effect
 158 of stationary planetary waves is included.

159 The linear model is used for analyzing the seasonal behavior of the tides in the
 160 GCM, which it reproduces reasonably well. We here focus on the three most relevant
 161 non-migrating tidal components. Perhaps least surprising is the important role
 162 played by condensation and convection in the forcing of DE3. An analysis of the
 163 seasonal cycle near the mesopause shows that the amplitude maximum between
 164 November and February is mostly due favorable propagation conditions given then
 165 by the zonal mean. *McLandress* (2002b) argues that the decisive factor in the modulation
 166 of the migrating tide by the zonal mean is the seasonal dependence of the
 167 zonal-mean vorticity in the background atmosphere. This might as well be the case
 168 for DE3. An erroneous maximum in HAMMONIA, as compared to observations,
 169 in August is prevented in the linear model by a counteracting effect due to the seasonal
 170 cycle in the forcing. The interplay between the zonal-mean background and
 171 the forcing thus seems to be essential for explaining the complete seasonal cycle.

172 Around the time of its maximum (April - June) *DS0* in the linear model is mostly
 173 excited by the direct non-migrating forcing by the absorption of short-wave solar

174 radiation and by condensational heating. Since the planetary waves are weak during
 175 this time it is no surprise that their effect is not so important then. Indeed, it is found
 176 that most of the seasonal cycle can be understood as an effect of variations in the
 177 zonal-mean background. However, this even holds between December and February
 178 when the planetary waves are strong. Closer analysis shows that the total signal is
 179 very similar to the direct non-migrating input from condensation and convection.
 180 Both, the effects from the direct non-migrating forcing by the absorption of solar
 181 short-wave radiation by tropospheric water vapor and the modulation of the migrat-
 182 ing forcing by the planetary waves are also strong, but cancel each other. It thus
 183 seems that destructive interference effects such as here might also be an essential
 184 factor of the planetary wave effect on non-migrating tides.

185 An example where the planetary waves actually enhance the amplitude of a non-
 186 migrating tide is *DW2*, as illustrated in Fig. 19.1. This tidal component is driven to a
 187 large proportion by the non-migrating forcing due to condensation and convection.
 188 The seasonal cycle can be explained to the largest part by the seasonal variations
 189 of the zonal-mean propagation conditions of this directly forced non-migrating tide.
 190 One also has, however, a quantitatively important impact from the planetary wave
 191 modulation of the migrating tide forced in the troposphere. This holds both for the
 192 total signal as such and for the simulated seasonal cycle. In conclusion, planetary
 193 waves do seem to be a factor to be taken into account in the dynamics of solar tides.

194 **19.3 Interaction between GWs and solar tides**

195 In previous efforts of tidal modeling (also see *Ortland and Alexander, 2006*, and ref-
 196 erence therein), the interaction between tides and GW parameterizations has been
 197 investigated under strong assumptions. Conventional GW parameterizations work
 198 in vertical columns which are assumed to be independent from each other, ignor-
 199 ing horizontal inhomogeneities in the large-scale flow (*McLandress, 1998*). Further-
 200 more, time-dependence of the large-scale background (BG) conditions is neglected.
 201 It is supposed that GW fields just see a quasi-stationary mean flow and adjust instan-
 202 taneously to its changes. In reality, however, GWs exhibit horizontal propagation
 203 and they are refracted at horizontal inhomogeneities of the BG. Time dependence
 204 of the latter changes the GW frequency. Furthermore, GWs propagate with a finite
 205 group velocity. Hence, if the time scale of the BG is short enough to get comparable
 206 to or smaller than the GW propagation time scale, significant deviations from the
 207 assumption of instantaneous adjustment appear. This might most likely be the case
 208 for solar tides in their effect on GW propagation.

209 In *Senf and Achatz (2011)* the effects of GW propagation and dissipation in real-
 210 istic tidal fields are investigated with the help of global ray-tracing simulations,
 211 thus extending the simplified calculations by *Eckermann and Marks (1996)*. In ray
 212 tracing (*Achatz et al., 2010, e.g.*), a locally monochromatic gravity wave field is
 213 propagated through a slowly changing environment. The GW field, or rather its lo-
 214 cal wave numbers and amplitudes are followed along characteristics, the so-called

215 rays, determined from the local group velocity (*Hasha et al.*, 2008, e.g.). The time-
 216 dependence of the BG wind, in our case the effect of the diurnal tide, induces a
 217 modulation of GW observed frequency along the ray. The horizontal gradients in
 218 the BG conditions lead to changes in the horizontal GW wave numbers. Following
 219 *Grimshaw* (1975), the GW amplitude is predicted from the conservation of wave ac-
 220 tion, supplemented by a damping rate estimated via the highly simplified saturation
 221 theory (*Lindzen*, 1981). Once a GW amplitude grows beyond the threshold at which
 222 it induces local overturning of isentropes it is forced back to this convective insta-
 223 bility threshold. Additionally, in the MLT region molecular viscosity and thermal
 224 diffusivity become more important and are included into the damping process. Our
 225 new global ray-tracer RAPAGI (RAY PArAmeterization of Gravity-wave Impacts)
 226 solves the ray-tracing equations on the sphere, using a small and highly idealized
 227 GW ensemble at source spectrum at 20km altitude. Each of the 14 individual and
 228 independent GW components is integrated forward separately. It has been shown
 229 by *Becker and Schmitz* (2003) that the mean residual circulation of the middle at-
 230 mosphere is well reproduced in a large-scale GCM when this GW ensemble is used
 231 in a classic parameterization according to *Lindzen* (1981). We note, however, that,
 232 as that mostly resulted from tuning, this GW ensemble is just one of many possi-
 233 bilities. Therefore, the simple GW ensemble is viewed as a reasonably-motivated
 234 toy configuration, while the analysis of even better chosen scenarios is left for the
 235 future.

236 The superposition of monthly means and tidal fields from the HAMMONIA
 237 model are chosen as background for three different off-line experiments, named
 238 "full", "noREF" and "TS", with decreasing complexity. The "full" experiment refers
 239 to a full ray-tracing simulation without any approximations for horizontal and time
 240 dependence. Thus, changes in frequency and all wave-number components appear
 241 and are induced by mean flow changes. The geographical distribution of the GW
 242 fields is altered as well. "noREF" (no refraction) is a simplified ray-tracing experi-
 243 ment in which neither horizontal refraction nor horizontal propagation are allowed.
 244 Only the vertical ray propagation is taken into account. Nonetheless, the rays have
 245 a finite group velocity and feel the transience of the BG wind. The horizontal wave-
 246 number components are constant along each ray, but frequency and vertical wave
 247 number vary to compensate temporal and vertical changes in the BG conditions,
 248 respectively. The third experiment is denoted by "TS" (time slicing) and equivalent
 249 to a classic single-column and steady-state parameterization. Only vertical varia-
 250 tions are taken into account. The tidal phase was fixed in 3h steps to sample the
 251 diurnal cycle, and finally the results from the different tidal phases were combined
 252 to a daily cycle. With the three experiments, effects of frequency modulation and
 253 the refraction of horizontal wave vector can be extracted. Differences between "TS"
 254 and "noREF" are attributed to the first, whereas differences between "noREF" and
 255 "full" to the latter. As the simpler simulations "TS" and "noREF" are obtained by
 256 successively simplifying the "full" one, a consistent comparison of the results is
 257 possible while keeping implementation aspects the same.

258 Since GW fields in the MLT region are periodically modulated by tidal winds,
 259 they produce a periodic force acting back on the diurnal tides. The relevant forc-

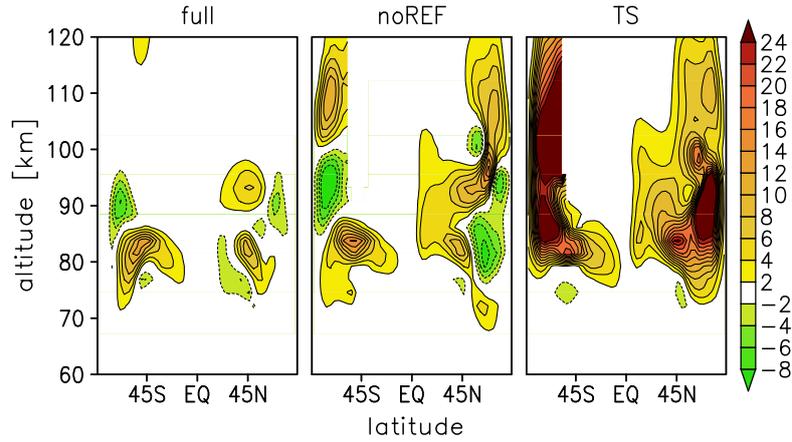


Fig. 19.2 The zonally averaged real part of the equivalent Rayleigh friction coefficient for the three different experiments: “full” (left), “noREF” (middle) and “TS” (right). The shading interval is $2 \times 10^{-6} \text{ s}^{-1}$.

260 ing of the mean flow, in our case temporally averaged flow plus diurnal tides, is
 261 given by the divergence of the pseudo-momentum fluxes from all 14 GW ensemble
 262 members. The diurnal amplitude of the zonal force can be analyzed most conven-
 263 niently on the basis of equivalent Rayleigh friction coefficients (ERFs). These have
 264 been introduced in the context of GW-tidal interaction by e.g. *Miyahara and Forbes*
 265 (1991) and further discussed e.g. by *McLandress* (2002a). With the help of ERFs,
 266 the effects of GWs can be incorporated into a linear tidal model. Effectively, the
 267 tidal component of the GW force is approximated by $f_\lambda \approx -\gamma_R u_T - \frac{\gamma_I}{\Omega} \partial_t u_T$, where
 268 u_T is the tidal wind, and γ_R and γ_I are the real and imaginary part of the ERFs, re-
 269 spectively. Positive real parts of the ERFs indicate regions of tidal damping and vice
 270 versa. The imaginary part of ERF acts on the tidal phase structure. A reduction of
 271 tidal vertical wave length is a very robust result in previous investigations, whereas
 272 the GW effect on tidal amplitudes is controversial (*Ortland and Alexander, 2006*,
 273 and references therein). The real parts of ERFs are shown in Fig. 19.2 for the three
 274 simulations. For the reference simulation “TS” in Fig. 19.2(c), large positive peaks
 275 up to $60 \times 10^{-6} \text{ s}^{-1}$ occur. The damping of tidal amplitudes is a quite typical result
 276 of Lindzen saturation parameterization. Others show qualitatively different effects
 277 on tides (e.g. *Ortland and Alexander, 2006*). For the “noREF” experiment, in Fig.
 278 19.2(b), the magnitude of γ_R is reduced. As analyzed in *Senf and Achatz* (2011)
 279 this results from an avoidance of critical levels, due to the time dependence of the
 280 tidal fields. The latitude-altitude structure is wave-like with a vertical wave length
 281 comparable to the tidal wave length. In Fig. 19.2(a), the magnitude of the ERF is
 282 further decreased. The influence of γ_R is drastically lowered at high latitudes and in
 283 the thermosphere. This is mostly due to the meridional refraction of the GW hori-
 284 zontal wave number by the mean wind gradients and the corresponding horizontal
 285 GW propagation (*Senf and Achatz, 2011*). The bottom line of this is that frequency

286 modulation and horizontal refraction by the tidal background significantly reduces
287 the GW forcing in the MLT.

288 **19.4 Conclusions**

289 The dynamics of solar tides is still a challenging field. We have here reported
290 progress on the linear modeling of these forced waves. This approach has the advan-
291 tage that cause-effect relationships can be established which would remain hidden in
292 an all-nonlinear approach. We are able to trace back characteristics of the seasonal
293 cycle of important components of the diurnal solar tide to the impact of either mi-
294 grating and non-migrating diurnal heating, or the impact of planetary waves on the
295 tidal propagation. The latter can lead to a non-migrating signal in the mesosphere,
296 caused by migrating forcing in the troposphere. An important problem remains the
297 GW-tidal interaction. So far we are able to show that it is incorrectly described on
298 the basis of single-column and steady-state GW parameterization approaches. The
299 time dependence of the solar tides, and the spatial gradients set by the background
300 atmosphere tend to reduce the GW impact much below what has been assumed so
301 far. The feedback on the tides, however, remains to be examined.

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